

Name:

Stuff You Must Know Cold – Calc BC

Limits

$\lim_{x \rightarrow a} f(x)$ exists if :

=

Theorems:

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} =$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} =$$

Steps:

- 1.
- 2.
- 3.

Definition of Continuity:

A function is continuous at the point $x=a$ if and only if:

- 1.
- 2.
- 3.

Vertical Asymptotes:

$$\lim_{x \rightarrow c} f(x) =$$

from either side of c .

Horizontal Asymptotes:

$$\lim_{x \rightarrow \pm\infty} f(x) =$$

Intermediate Value Theorem

Extreme Value Theorem

Rolle's Theorem

Derivatives

Definition of Derivative

$$\frac{d}{dx}(f(x)) =$$

Alternate Form of Def. of Derivative

$$\frac{d}{dx}(f(x)) \text{ at } x = a$$

Equation of a tangent line at $x=a$

Chain Rule

$$f(g(x))$$

Product Rule

$$f \cdot g$$

Quotient Rule

$$\frac{f}{g}$$

Curve Sketching and Analysis

Critical Points:

Increasing:

Decreasing:

Relative Min:

Relative Max:

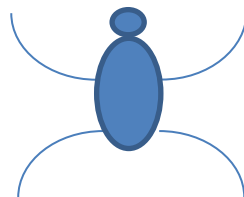
Absolute Extrema:

Check endpoints! Candidates test or global argument.

Concave Up:

Concave Down:

Point of Inflection:



More Derivatives

Where u is a function of x and a is a constant

function	derivative
x^n	
$\sin u$	
$\cos u$	
$\tan u$	
$\csc u$	
$\sec u$	
$\cot u$	
$\arcsin u$	
$\arccos u$	
$\arctan u$	
$\operatorname{arccsc} u$	
$\operatorname{arcsec} u$	
$\operatorname{arccot} u$	
e^u	
$\ln u$	
a^u	
$\log_a u$	

Derivative of an Inverse

(a,b) on $f(x)$

$$g(x) = f^{-1}(x)$$

$$g'(b) =$$

The Mean Value Theorem

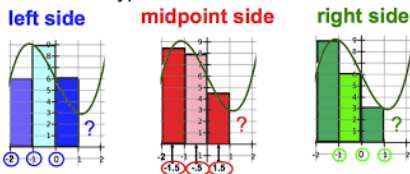
(derivatives)

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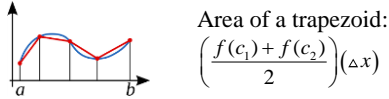
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Riemann Sums:

3 types of Riemann Sums



Trapezoidal Sum:



Limit definition of an Integral:

$$\text{Area} = \int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n [f(c_i) \Delta x]; \quad \Delta x = \frac{b-a}{n}$$

The Fundamental Theorem of Calculus

$$\int_a^b f(x) dx = F(b) - F(a)$$

$$F'(x) = f(x)$$

Corollary to FTC

$$\frac{d}{dx} \int_{h(x)}^{g(x)} f(t) dt = f[g(x)]g'(x) - f[h(x)]h'(x)$$

Mean Value Theorem for Integrals
(Average Value)

$$\frac{\int_a^b f(x) dx}{b-a}$$

Other integration rules:

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int \tan u du = -\ln |\cos u| + C$$

$$\int \sec u du = \ln |\sec u + \tan u| + C$$

$$\int \csc u du = -\ln |\csc u + \cot u| + C$$

$$\int \cot u du = \ln |\sin x| + C$$

$$\int a^u du = \frac{a^u}{\ln a} + C$$

Integration by Parts

$$\int u dv = uv - \int v du$$

L'Hôpital's Rule :

$$\lim_{x \rightarrow c} \frac{f(x)}{g(x)}$$

If $\lim_{x \rightarrow c} f(x) = 0$ or ∞ , and $\lim_{x \rightarrow c} g(x) = 0$ or ∞ ,

then $\lim_{x \rightarrow c} \frac{f(x)}{g(x)} =$

Euler's Method

N	X _n	Y _n	$\frac{dy}{dx} \Big _n$

$$x_{n+1} =$$

$$y_{n+1} =$$

Logistics

$$\frac{dP}{dt} =$$

$$P =$$

$$b = \quad \lim_{t \rightarrow \infty} P(t) =$$

Population is increasing the fastest at

Area between two curves:

Volumes of Known Cross Sections:

$$\int_a^b (\text{Area with respect to } s) dx$$

$s = \text{Top} - \text{Bottom}$
(Perpendicular to x-axis)

$$\int_a^b (\text{Area with respect to } s) dy$$

$s = \text{Right} - \text{Left}$
(Perpendicular to y-axis)

Squares:

Rectangles:

Equilateral Triangles:

Isosceles Right Triangles:

Semicircles:

Series Convergence Tests:

Solids of Revolution

Disk Method

Washer Method

Arc Length
(rectangular)

(parametric)

(polar)

Parametric Equations

$$\frac{dy}{dx} =$$

$$\frac{d^2y}{dx^2} =$$

Distance, Velocity, and Acceleration

$s(t)$ is the position function,
< $x(t), y(t)$ > is the position vector

velocity =

acceleration =

speed = =

velocity vector =

acceleration vector =

Speed is increasing _____.

position =

Total distance

average velocity =

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Polar Curves

Area =

$$\frac{dy}{dx} =$$

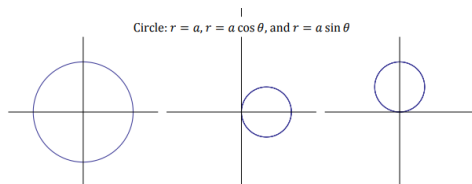
x = y =

Slope =

Basic Polar Curves:

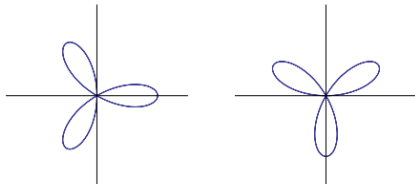
Circle:

Circle: $r = a$, $r = a \cos \theta$, and $r = a \sin \theta$

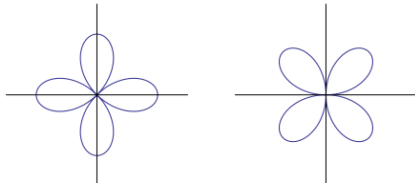


Rose:

Three-leaved rose: $r = a \cos 3\theta$ and $r = a \sin 3\theta$

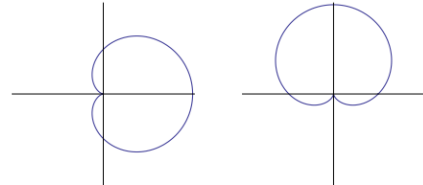


Four-leaved rose: $r = a \cos 2\theta$ and $r = a \sin 2\theta$

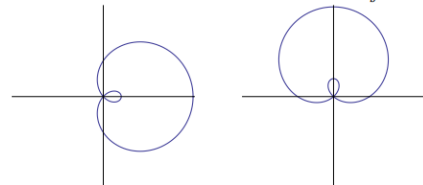


Limacons:

Cardioid: $r = a + a \cos \theta$ and $r = a + a \sin \theta$

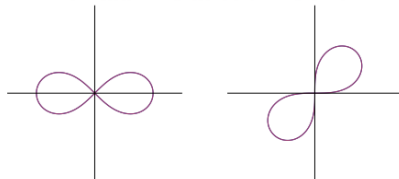


Limaçon: $r = a + b \cos \theta$ and $r = a + b \sin \theta$ where $\frac{a}{b} < 1$



Lemniscates:

Lemniscate: $r^2 = a^2 \cos 2\theta$ and $r^2 = a^2 \sin 2\theta$



Nth Term

Geometric

P-Series

Alternating Series Test

Direct Comparison

Limit Comparison

Integral Test

Ratio Test

Taylor Series

$$y = \sin x$$

Maclaurin Series

Series you need to memorize:

$$e^x =$$

$$\cos x =$$

$$\sin x =$$

$$\frac{1}{1-x} =$$

Alternating Remainder

Lagrange Error

Trig

Signs: All Students Take Calculus

sin	All functions are positive
csc	

tan	cos
cot	sec

Values:

	30°	45°	60°
sin θ			
cos θ			
tan θ			

Quadrants

(cos, sin)
tan = sin/cos

Trig Graphs:

$$y = \cos x$$

$$y = \tan x$$

Pythagorean Identities:

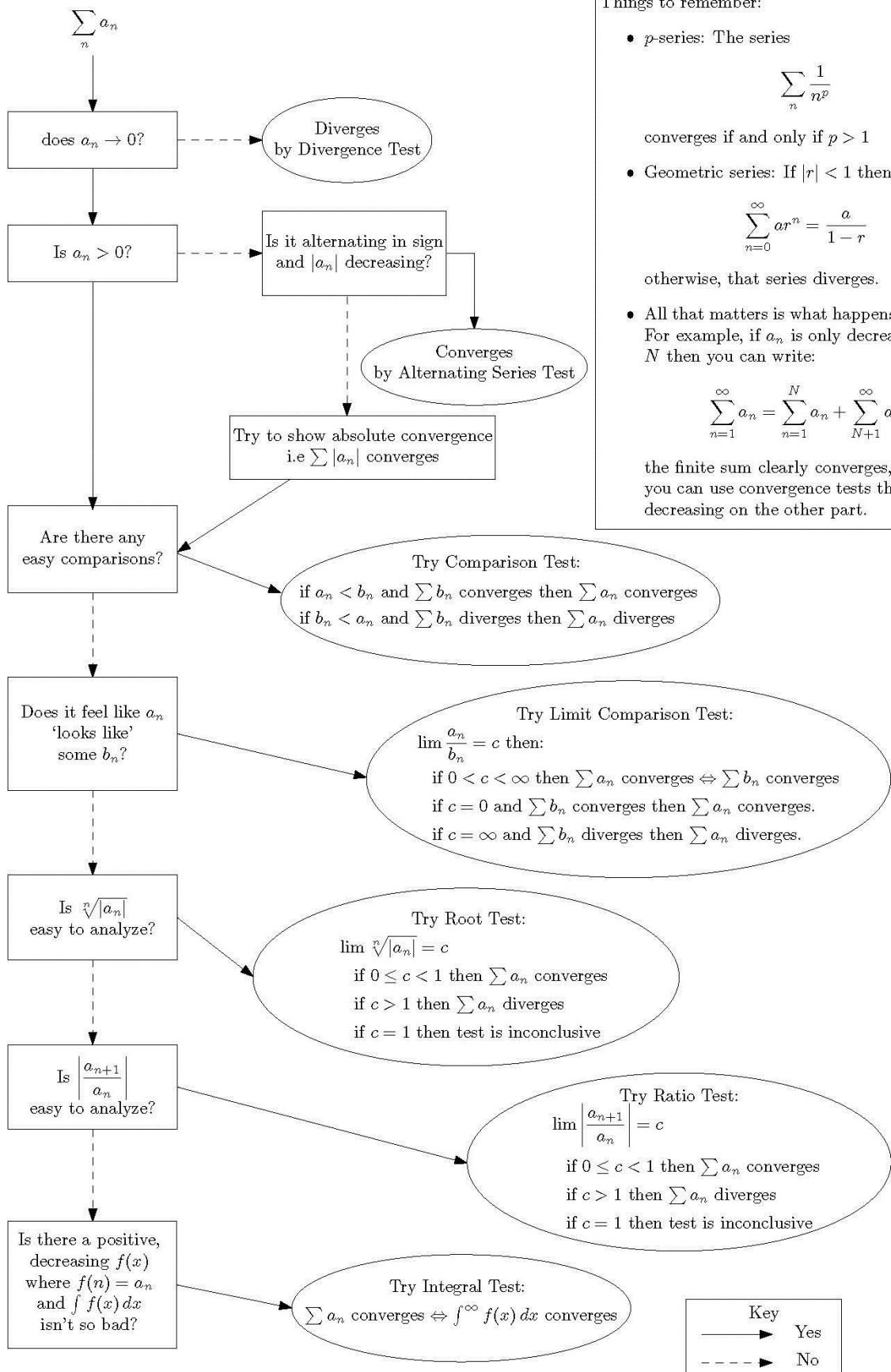
• **Reciprocal Identities:**

Double Angles:

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Series Convergence Flowchart



Things to remember:

- p -series: The series $\sum_n \frac{1}{n^p}$ converges if and only if $p > 1$
- Geometric series: If $|r| < 1$ then $\sum_{n=0}^{\infty} ar^n = \frac{a}{1-r}$ otherwise, that series diverges.
- All that matters is what happens on a tail. For example, if a_n is only decreasing after N then you can write: $\sum_{n=1}^{\infty} a_n = \sum_{n=1}^N a_n + \sum_{n=N+1}^{\infty} a_n$ the finite sum clearly converges, and then you can use convergence tests that require decreasing on the other part.